

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+)	Page 1
	End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2	
	for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Version 2
		26. Jan. 2021

ESA Climate Change Initiative “Plus” (CCI+)

End-to-End ECV Uncertainty Budget Version 2 (E3UBv2)

-

for the FOCAL XCO₂ OCO-2 Data Product CO₂_OC₂_FOCA

for the Essential Climate Variable (ECV)
Greenhouse Gases (GHG)

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 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 2
		Version 2
		26. Jan. 2021

Change log

Version Nr.	Date	Status	Reason for change
Version 1 draft	29. Nov. 2019	Submitted for review	New document
Version 1	6. Jan. 2020	Final / submitted	Improved Fig. 5
Version 2 draft	16. Nov. 2020	Submitted for review	New data set FOCAL v09 2015-2019
Version 2	25. Jan. 2021	Final	Modified discussion, new Fig. 4.1

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 3
		Version 2
		26. Jan. 2021

Table of Contents

1	Introduction	4
1.1	Purpose of document	4
1.2	Intended audience	4
2	Uncertainty analysis based on simulations	5
3	Comparison with CAMS model results	9
4	Comparison with NASA’s operational OCO-2 L2 product	12
5	Validation with TCCON	15
5.1	XCO ₂	15
5.2	XCO ₂ uncertainty	21
	Acknowledgements	23
	References	24

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 4
		Version 2
		26. Jan. 2021

1 Introduction

1.1 Purpose of document

This document describes the End-to-End ECV Uncertainty Budget (E3UB) of the FOCAL OCO-2 XCO₂ product. It provides an overview of random and systematic errors affecting the FOCAL OCO-2 XCO₂ L2 product. Reliable uncertainty estimates of the retrieval are required to translate remotely sensed data into modelled estimations with a known degree of confidence, allowing, e.g., the detection of climate change impacts additional to the natural variability of greenhouse gases. In particular, the GHG-CCI User Requirements have placed strict measurement accuracy and precision requirements on the participating GHG retrievals, allowing identification of minute changes in magnitude and sign of XCO₂ concentration change (*/URDv3.0, 2020/*).

1.2 Intended audience

This document is intended for users in the modelling community applying IUIP's FOCAL OCO-2 XCO₂ L2 product for CO₂ inversions, as well as remote sensing experts interested in atmospheric soundings of XCO₂. In both cases, the work presented here will give the user a more thorough understanding of uncertainties implicit in this GHG-CCI+ product.

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 5
		Version 2
		26. Jan. 2021

2 Uncertainty analysis based on simulations

This section summarizes the results shown in section 7 of FOCAL’s */ATBDv1/* which, in turn, bases on the publication of */Reuter et al., 2017a/*, in parts.

In order to asses FOCAL’s theoretical capabilities (primarily in retrieving XCO₂, XH₂O, and SIF), */Reuter et al., 2017a/* confronted it with radiance measurements simulated with the accurate RT code SCIATRAN */Rozanov et al., 2014/*. The performed analyses can be understood also as test of the suitability of the approximations made in FOCAL’s RT and of the retrieval setup. Hereby, they primarily concentrated on scattering related errors and analyzed the systematic and stochastic, i.e., the a posteriori errors of several different geophysical scenarios and retrieval setups. They were not aiming to comprehensively cover the majority of potential geophysical scenarios, because the final quality depends on the full retrieval scheme including, e.g., potential instrument and forward model errors and different post-filtering capabilities. The aim of their retrieval experiments, summarized in this section, was rather to identify a retrieval setup which is a promising candidate for a full retrieval scheme and its application to actually measured OCO-2 data. Their 3-Scat retrieval setup (see */Reuter et al., 2017a/* for details) showed often relatively low systematic XCO₂ and XH₂O errors with low polarization dependency, well controlled retrieved profiles, lowest CO₂ smoothing errors, a relatively realistic a priori error correlation matrix for CO₂, and advantageous AKs. Therefore, they identified this retrieval setup as promising candidate which, in turn, became the basis for FOCAL v8.

The 3-Scat setup fits the OCO-2 measured radiance in four fit windows by simultaneously retrieving the following geophysical parameters: five layered CO₂ and H₂O concentration profiles, the pressure (i.e., height), scattering optical thickness at 760 nm, and the Ångström exponent of a scattering layer, SIF, and polynomial coefficients describing the spectral albedo in each fit window.

As accurate XCO₂ retrievals will probably always require a rigorous cloud and aerosol screening, */Reuter et al., 2017a/* concentrated on scenarios with scattering optical thicknesses in the range of about 0.03 and 0.70. The quality of the spectral fits in the O₂ fit window was usually 2.5 to 4 times better than expected from instrumental noise. In the CO₂ fit windows, the quality of the spectral fits was usually at least 7 times better than expected from instrumental noise and even smaller fit residuals were obtained in the SIF fit window.

Figure 2.1 shows some example fit residuals.

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 6
		Version 2
		26. Jan. 2021

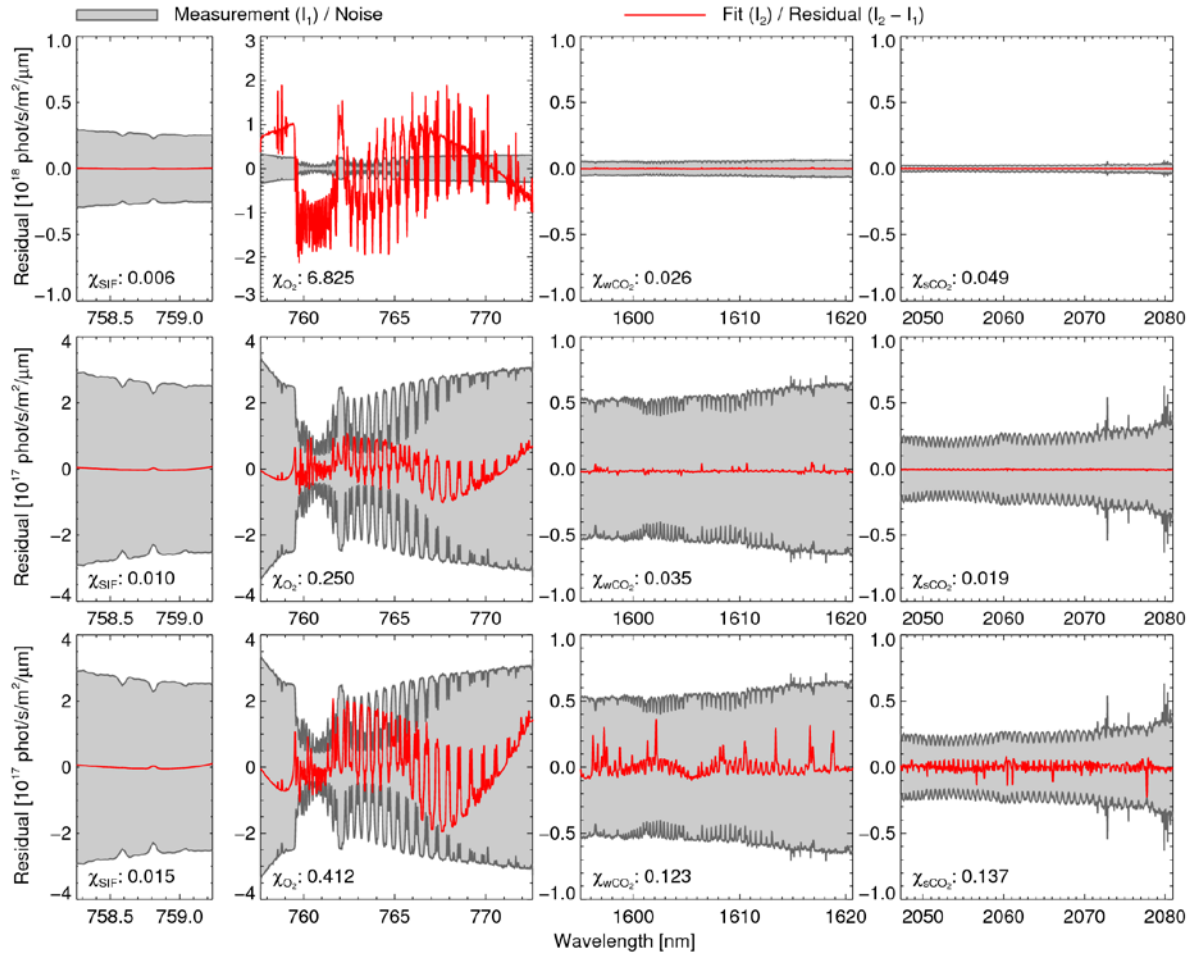


Figure 2.1: Residuals (fit minus measurement, **red**) and measurement noise (**gray**) of SCIATRAN simulated OCO-2 measurements fitted with FOCAL (solar zenith angle = 40°, parallel polarization). **Top:** Rayleigh scenario and the 0-Scat setup (allowing not the fitting of scattering parameters). **Middle:** Rayleigh scenario and the 3-Scat setup. Bottom: Rayleigh+Aerosol/BG+Water cloud scenario and the 3-Scat setup. See [Reuter et al., 2017a/](#) for details on the geophysical scenarios and retrieval setups.

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 7
		Version 2
		26. Jan. 2021

Systematic errors of XCO_2 ranged from -2.5 ppm to 3.0 ppm and were usually smaller than ± 0.3 ppm (for the tested scenarios). The stochastic uncertainty of XCO_2 was typically about 1.0 ppm (**Figure 2.2**). Systematic errors of XH_2O ranged from -243 ppm to 0 ppm and were usually smaller than ± 6 ppm. The stochastic uncertainty of XH_2O was typically about 9 ppm. Note, 1000 ppmb correspond to 6.44 kg/m^2 for the analyzed H_2O profiles. The degree of freedom for the retrieved five-layered CO_2 and H_2O profiles was typically 2.2. As SIF is retrieved from Fraunhofer lines in a spectral region with negligible gaseous absorption features, it can be retrieved without significant interferences with the retrieved scattering properties. The systematic SIF errors were always below $0.02 \text{ mW/m}^2/\text{sr/nm}$. Therefore, **/Reuter et al., 2017a/** expected that instrumental or forward model effects causing an in-filling (a reduction of the line depths) of the used Fraunhofer lines will dominate the systematic errors when analyzing actually measured data. The stochastic uncertainty of SIF was usually below $0.3 \text{ mW/m}^2/\text{sr/nm}$.

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 8
		Version 2
		26. Jan. 2021

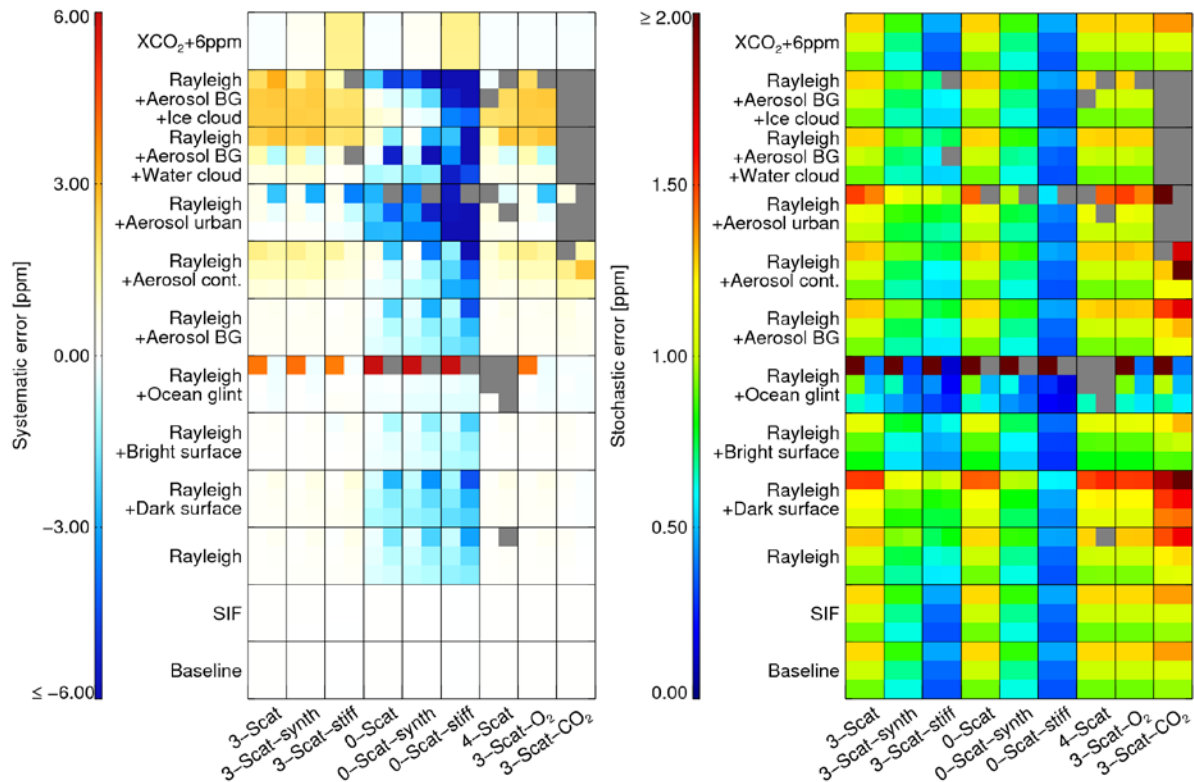


Figure 2.2: Error characteristics of nine retrieval setups and twelve geophysical scenarios. Each box includes six sub-boxes representing polarization parallel (left) and perpendicular (right) to the SPP as well as three solar zenith angles (20°, 40°, and 60°, from bottom to top). Gray boxes represent not converging retrievals. **Left:** Systematic error (retrieved minus true XCO₂). **Right:** Stochastic uncertainty as reported by the optimal estimation retrieval. See [/Reuter et al., 2017a/](#) for details on the geophysical scenarios and retrieval setups.

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 9
		Version 2
		26. Jan. 2021

3 Comparison with CAMS model results

This section bases on section 8.1 of FOCAL’s **/ATBDv1, 2019/** which, in turn, summarizes results of a comparison of FOCAL v06 with the CAMS model done by **/Reuter et al., 2017b/**.

Here we compare one year (2015) of post-filtered and bias corrected FOCAL v09 XCO₂ results with corresponding values of the CAMS v15r4 model accounting for FOCAL’s column averaging kernels (e.g., **/Rodgers, 2000/**). **Figure 3.1** shows 5°×5°monthly gridded values for six months (Feb., Apr., Jun., Aug., Oct., and Dec. 2015) of FOCAL data and **Figure 3.2** shows corresponding values of CAMS v15r4 data. The main spatial and temporal patterns are similar for FOCAL and CAMS with largest and smallest values in the northern hemisphere in April and August, respectively. Differences become larger at smaller scales, e.g., FOCAL sees larger values in natural and anthropogenic source regions of Sub-Saharan Africa and East Asia, e.g., in April but also above the Sahara, e.g., in August. However, it shall be noted that often only few data points are in the corresponding grid boxes.

In grid boxes with more than 100 soundings, the standard error of the mean becomes negligible (~0.1ppm). Therefore, the difference between FOCAL and CAMS in such grid boxes can be interpreted as systematic temporal and regional mismatch or bias. The heatmap shown in **Figure 4.1** (left) bases on these grid boxes. The standard deviation of this systematic mismatch (including also representation errors) amounts to 1.0ppm and the correlation between FOCAL and CAMS is 0.88.

The standard deviation of the single sounding mismatch after subtracting the systematic mismatch amounts to 1.2 ppm which is consistent with the average reported uncertainty of 1.2 ppm.

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 10
		Version 2
		26. Jan. 2021

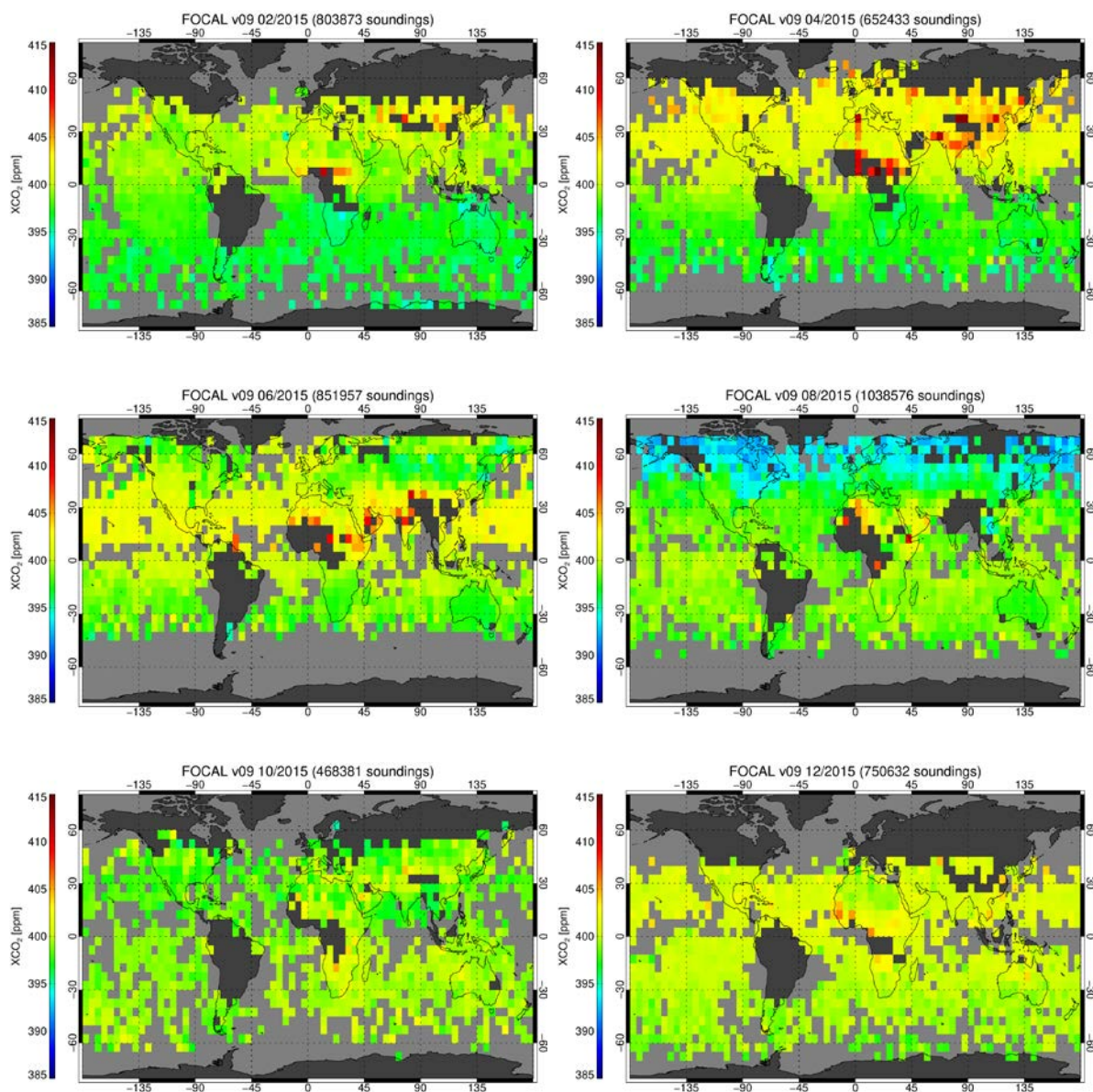


Figure 3.1: FOCAL v09 monthly mean XCO₂ gridded to 5°x5°. From top/left to bottom/right: Feb., Apr., Jun., Aug., Oct., and Dec. 2015.

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+)	Page 11
	End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2	Version 2
	for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	26. Jan. 2021

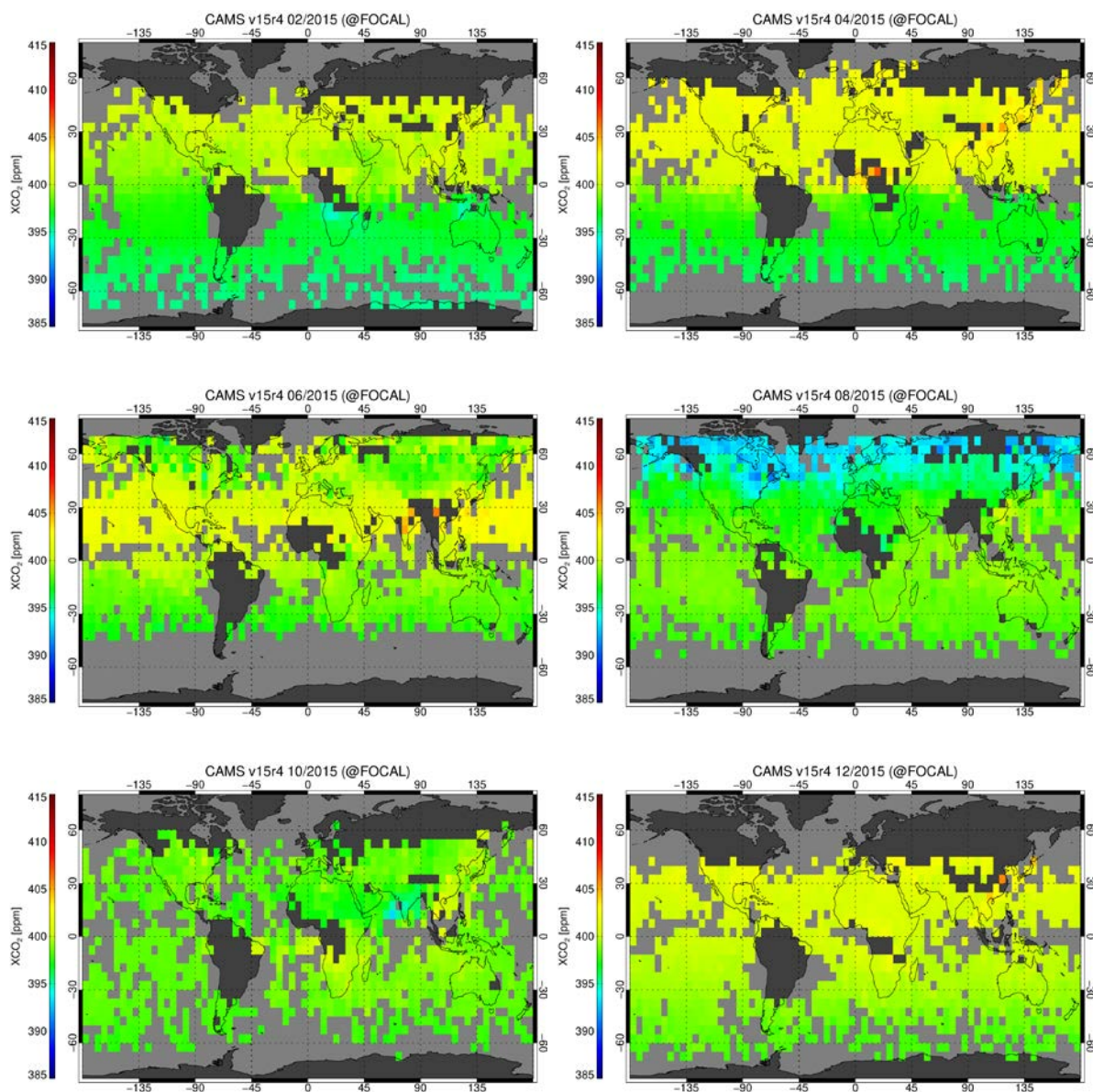


Figure 3.2: CAMS v15r4 monthly mean XCO₂ sampled as FOCAL and gridded to 5°x5°. From top/left to bottom/right: Feb., Apr., Jun., Aug., Oct., and Dec. 2015.

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 12
		Version 2
		26. Jan. 2021

4 Comparison with NASA’s operational OCO-2 L2 product

In this section we compare the same year of post-filtered and bias corrected FOCAL v09 XCO₂ results with NASA’s operational OCO-2 L2 product v10.2. Our comparison method is similar to what has been done in Section 3. However, as FOCAL and the NASA product feature different samplings, we first gridded the NASA product and compared FOCAL with corresponding grid box averages. In order to improve the comparability, both data products have been adjusted for a common a priori **/Rodgers, 2000/** namely SECM2020 **/Reuter et al., 2012/**.

Comparing **Figure 3.1** with **Figure 4.2** shows similar large scale temporal and spatial patterns and also the relative enhancement in the anthropogenic source regions of East Asia in April are similar. The most obvious difference is that the NASA product has about three times more soundings. The primary reason for this is the inherently poor throughput (~11%) of the MODIS based cloud screening of FOCAL’s preprocessor **/Reuter et al., 2017b/**. Additionally, one can observe a larger variability in the gridded FOCAL product which can only partly be explained by the sparser filling of the grid boxes.

Similarly, as done for the model comparison, we concentrate only on grid boxes with more than 100 FOCAL and NASA soundings so that the standard error of the mean becomes negligible (~0.1ppm). Therefore, the difference between FOCAL and NASA in such grid boxes can be interpreted as systematic temporal and regional mismatch or bias. The heatmap shown in **Figure 4.1** (right) bases on these grid boxes. The standard deviation of this systematic mismatch (including also representation errors) amounts to 1.0ppm and the correlation between FOCAL and NASA is 0.89.

FOCAL scatters within the grid boxes with a standard deviation of 1.3ppm which is similar to the average reported uncertainty of 1.2ppm.

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 13
		Version 2
		26. Jan. 2021

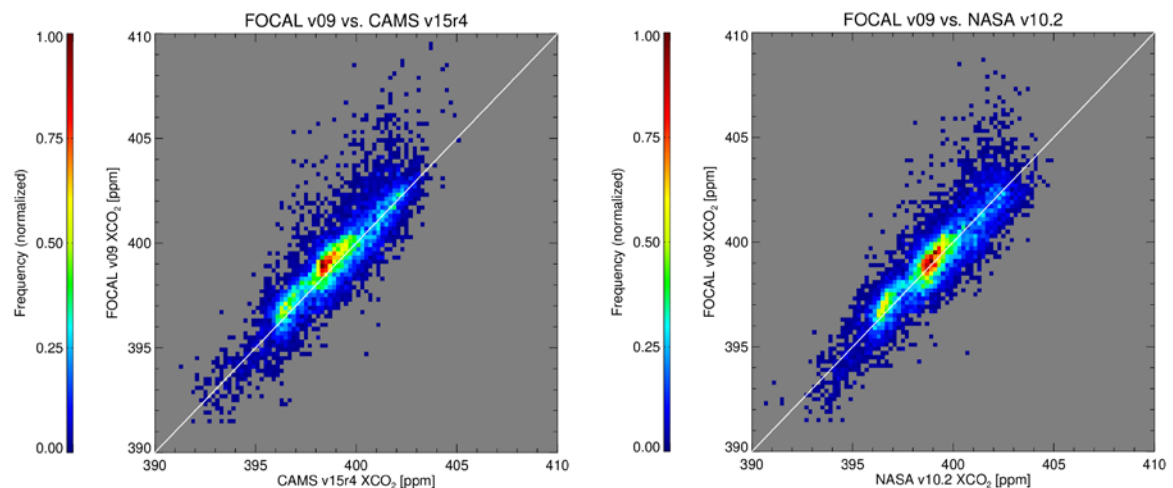


Figure 4.1: Heat maps of FOCAL v09 vs. CAMS v15r4 XCO₂ data (left) and FOCAL v09 vs. NASA v10.2 XCO₂ data (right) on the basis monthly 5°×5° grid boxes including more than 100 data points.

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+)	Page 14
	End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2	
		Version 2
		26. Jan. 2021
for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)		

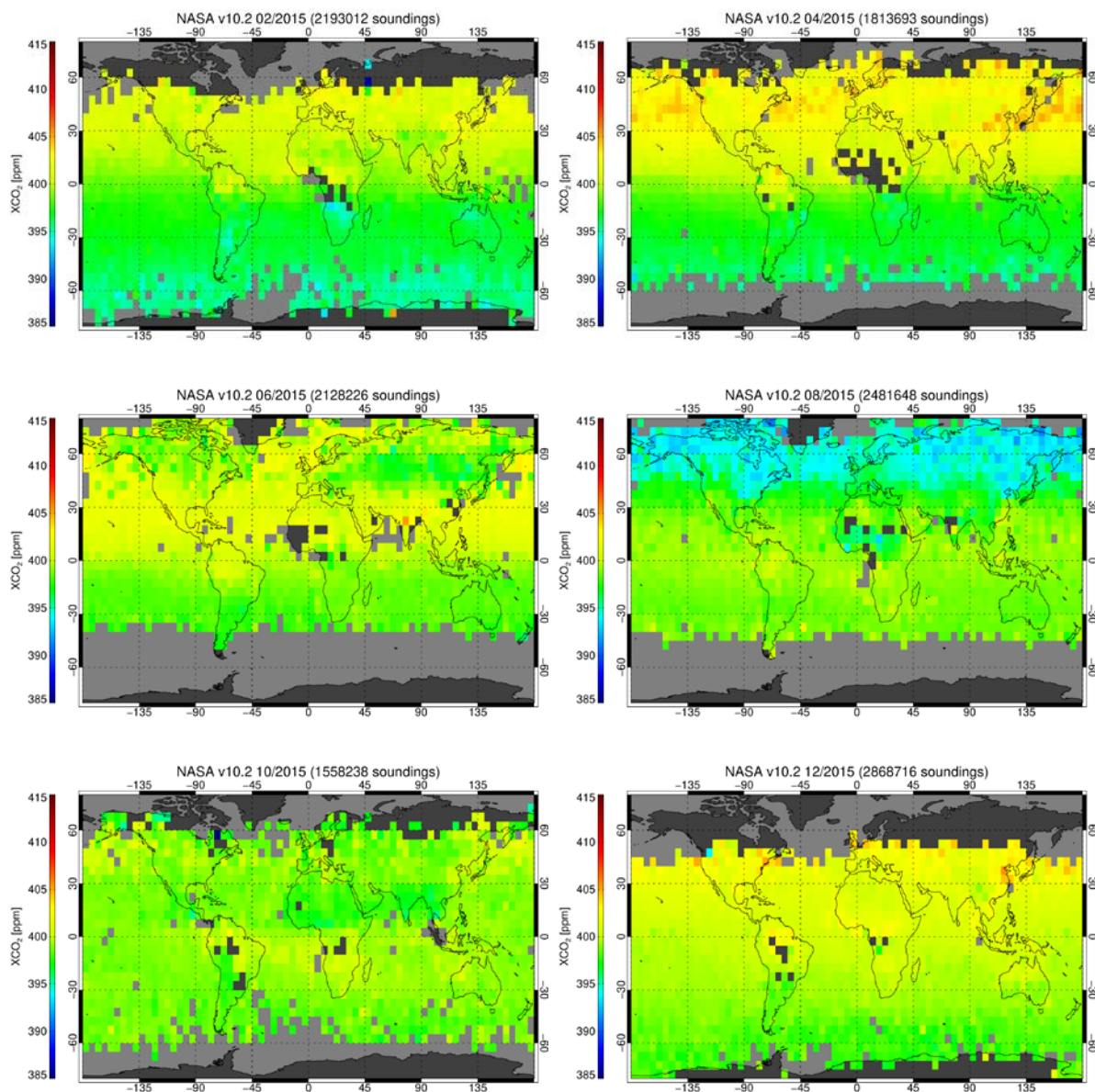


Figure 4.2: As Figure 3.1 but for NASA’s operational OCO-2 v10.2 L2 product.

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 15
		Version 2
		26. Jan. 2021

5 Validation with TCCON

The validation results shown in this section are valid for FOCAL v09. The applied methods are similar to those described in BESD's Comprehensive Error Characterisation Report **/CECRv3, 2017/** and the Product Validation and Intercomparison Report **/PVIRv5, 2017/** of ESA's GHG CCI project and partly also in the publication of **/Reuter et al., 2011/**. For all comparisons, averaging kernels have been applied as described in the C3S GHG Product User Guide and Specification **/PUGS, 2019/**.

5.1 XCO₂

FOCAL's XCO₂ has been validated with TCCON GGG2014 measurements. The co-location criteria are defined by a maximum time difference of two hours, a maximum spatial distance of 500km, and a maximum surface elevation difference of 250m. **Figure 5.1** shows all co-located FOCAL and TCCON retrievals of the years 2015-2019 for TCCON sites with more than 250 co-locations and covering a time period of at least two years. One can see that FOCAL captures the year-to-year increase and the seasonal features. For each station, the performance statistics number of co- locations, station bias, seasonal bias, linear drift, and single measurement precision were calculated.

We define the station bias as average difference to TCCON. Seasonal bias, linear drift, and single sounding precision have been derived by fitting the following trend model:

$$\Delta X = a_0 + a_1 t + a_2 \sin(2\pi t + a_3) + \varepsilon \quad (5-1)$$

Here, ΔX represents the difference satellite minus TCCON , and a_{0-3} the free fit parameters. Specifically, a_1 represents the linear drift and a_2 the amplitude of the seasonal bias. The single sounding precision is computed by the standard deviation of the residua ε .

Based on the per station statistics, the following summarizing statistics have been calculated: Total number of co-locations used for validation, average single measurement precision, station-to-station bias (standard deviation of the station biases), average seasonal bias (standard deviation of the seasonal bias term), and average linear drift. As the linear drift can be assumed to be globally constant, the station-to-station standard deviation of the linear drift is a measure for its uncertainty. Per station statistics and overall performance estimates are listed in **Table 1**.

In total, more than 700000 co-located FOCAL measurements have been used for the validation exercise. The overall single measurement precision is 1.48ppm and station-to-station biases amount to 0.57ppm.

In the context of station-to-station biases, it shall be noted that **/Wunch et al., 2010, 2011/** specifies the accuracy (1σ) of TCCON to be about 0.4ppm. This means it cannot be expected to find regional biases considerably less than 0.4ppm using TCCON as reference.

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 16
		Version 2
		26. Jan. 2021

Seasonal cycle biases amount to 0.37ppm on average and no significant (temporally linear) drift can be found ($0.03 \pm 0.26 \text{ ppm/a}$).

Additionally, a measure for the year-to-year stability has been computed as follows. For each TCCON site, the residual difference (satellite - TCCON) which is not explained by station bias, seasonal bias, and/or linear drift has been derived by subtracting the fit of the bias model ΔX from the satellite minus TCCON difference. These time series were smoothed by a running average of 365 days. Only days where more than 10 co-locations contributed to the running average of at least 5 TCCON sites have been further considered. At these days, the station-to-station average has been calculated. The corresponding expected uncertainty has been computed from the standard error of the mean (derived from the station-to-station standard deviation and the number of stations) and by error propagation of the reported single sounding uncertainties. For FOCAL, the average is always between about -0.2ppm and 0.2ppm (**Figure 5.2**) with an uncertainty of typically about 0.15ppm. Most of the time, the average is not significantly different from zero, i.e., its one sigma uncertainty is larger than its absolute value. Due to the relatively large uncertainty, we decided to compute not the maximum minus minimum as a measure for the year-to-year stability because this quantity can be expected to increase with length of the time series simply due to statistics. Therefore, we estimate the year-to-year stability by randomly selecting pairs of dates with a time difference of at least 365 days. For each selection we computed the difference modified by a random component corresponding to the estimated uncertainty. From 1000 of such pairs we compute the standard deviation as estimate for the year-to-year stability. We repeat this experiment 1000 times and compute the average (0.18ppm) and standard deviation (0.01ppm).

From this, we conclude that the year-to-year stability is 0.18ppm/a (**Figure 5.2**).



GHG-CCI+ project

ESA Climate Change Initiative "Plus" (CCI+)

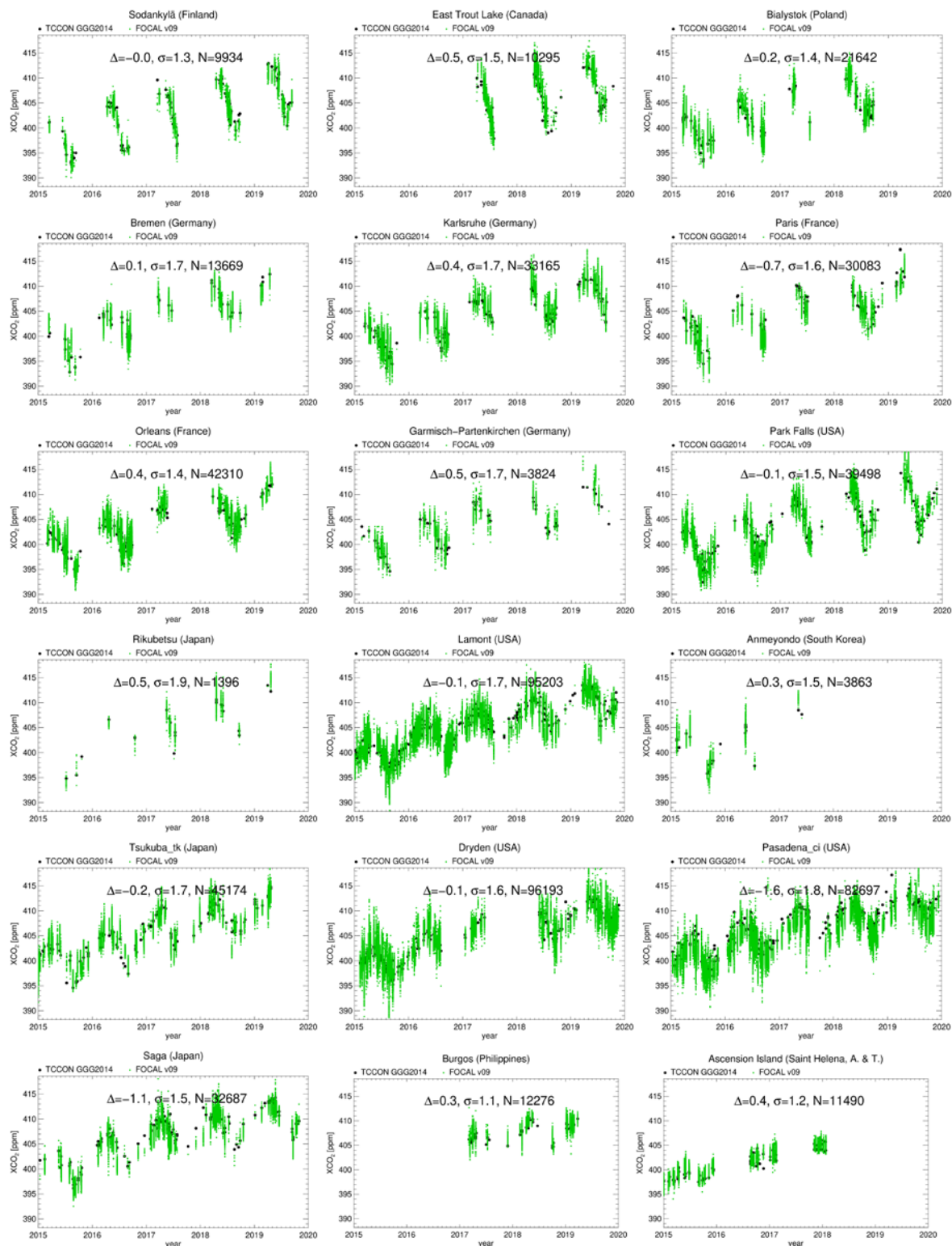
End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2

for the Essential Climate Variable (ECV)
Greenhouse Gases (GHG)

Page 17

Version 2

26. Jan. 2021



 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 18
		Version 2
		26. Jan. 2021

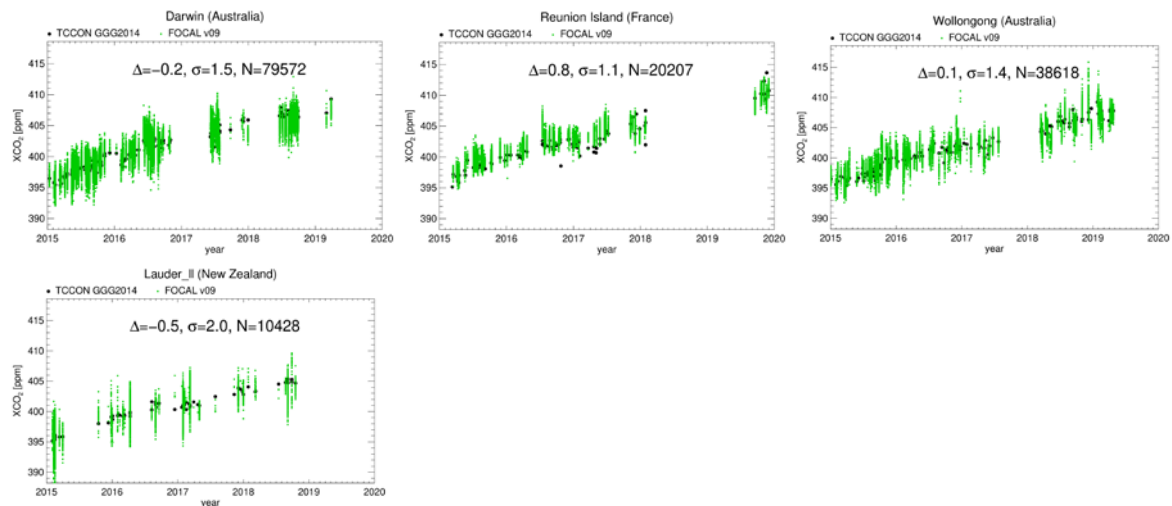


Figure 5.1: Validation of single soundings of FOCAL (**green**) with co-located TCCON measurements (**black**) at all TCCON sites with more than 250 co-locations and covering a time period of at least one year. Numbers in the figures: Δ = station bias, i.e., average of the difference; σ = single measurement precision, i.e., standard deviation of the difference; N = number of co-locations. From top/left to bottom/right the TCCON sites have been sorted by latitude.

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+)	Page 19
	End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Version 2
		26. Jan. 2021

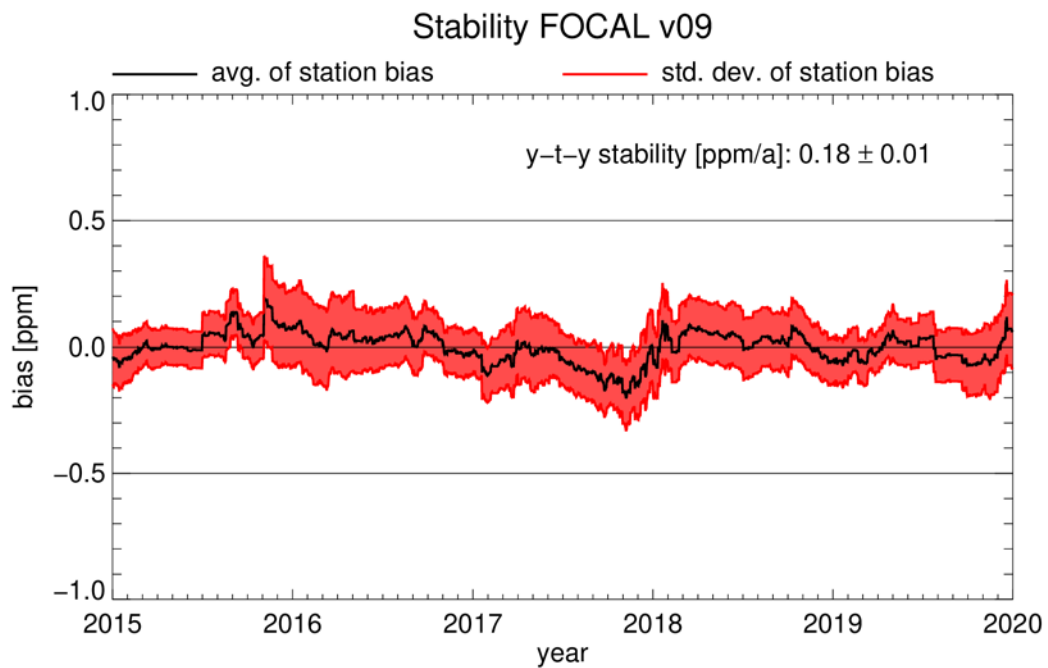


Figure 5.2: Stability analyses for FOCAL. The black curve shows the average station bias and the red curves its uncertainty represented by the station-to-station standard deviation and error propagation from single sounding measurement noise.

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 20
		Version 2
		26. Jan. 2021

Table 1: Validation statistics for all TCCON sites with more than 250 co-locations and covering a time period of at least two years with number of co-locations (#col), number of days with co-locations (#day), single measurement precision (σ), station bias (Δ), seasonal bias (s) and linear drift (d). The last row contains the overall statistics. In this row σ represents the (quadratic) average single measurement precision, Δ the station-to-station bias (i.e., the standard deviation of the station biases), s the average seasonal bias, and d the average drift plus minus its standard deviation.

Station	#col	#day	σ [ppm]	Δ [ppm]	s [ppm]	d [ppm/a]
Sodankylä	9934	119	1.25	-0.03	0.28	-0.08
East Trout Lake	10295	79	1.43	0.48	0.43	0.22
Bialystok	21642	101	1.43	0.24	0.12	0.14
Bremen	13669	45	1.56	0.10	0.67	-0.20
Karlsruhe	33165	129	1.52	0.43	0.68	0.15
Paris	30083	77	1.57	-0.75	0.36	0.01
Orleans	42310	131	1.36	0.45	0.20	-0.07
Garmisch-P.	3824	70	1.62	0.54	0.57	0.27
Park Falls	39498	197	1.39	-0.07	0.53	0.15
Rikubetsu	1396	18	1.64	0.49	0.58	0.83
Lamont	95203	256	1.63	-0.11	0.25	-0.06
Anmeyondo	3863	18	1.44	0.31	0.28	-0.20
Tsukuba	45174	103	1.65	-0.22	0.37	-0.10
Dryden	96193	178	1.57	-0.12	0.34	-0.18
Pasadena	82697	255	1.74	-1.59	0.30	-0.08
Saga	32687	104	1.54	-1.13	0.10	0.12
Burgos	12276	33	1.01	0.35	0.32	0.15
Ascension Island	11490	61	1.13	0.36	0.22	0.16
Darwin	79572	146	1.37	-0.19	0.18	-0.37
Reunion Island	20207	78	1.01	0.77	0.27	-0.27
Wollongong	38618	123	1.38	0.15	0.22	-0.22
Lauder	10428	48	1.89	-0.46	0.76	0.30
Total	600174	2369	1.48	0.57	0.37	0.03±0.26

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 21
		Version 2
		26. Jan. 2021

5.2 XCO₂ uncertainty

Especially for the application of flux inversion, reliable information on the uncertainty of each individual sounding is necessary. For this purpose, we analyzed the same validation dataset of co-located FOCAL and TCCON measurements also used in Section 5.1.

For each co-location used for the validation shown in Section 5.1, we have a residual ε of the bias model ΔX . From this, we computed our best estimate for the stochastic uncertainty (precision) as it does not include the analyzed systematic biases (trend, seasonal cycle, station-to-station).

For each ε , we have a corresponding uncertainty reported by FOCAL’s optimal estimation retrieval. We pooled the entire data set of more than 700000 co-locations into 20 bins with increasing reported uncertainty in a way that each bin included the same number of co-locations. For each bin, we computed the (quadratic) average reported uncertainty and the standard deviation of the residual ε (actual precision).

Figure 5.3 shows that both quantities are connected by a fairly linear relationship. However it shall be notated, that the reported uncertainty is mainly driven by the instrumental noise which is in turn driven by the radiance so that the darkest scenes usually have the largest reported uncertainties. This means, especially the bins including the largest (or smallest) reported uncertainties may be dominated by an individual validation site with especially dark (or bright) albedo, while the other bins usually consist of data from a larger mixture of TCCON sites.

The linear fit shown in **Figure 5.3** shows that FOCAL’s reported uncertainties has a positive correlation with the actual precision but it shows also that FOCAL’s reported uncertainty is somewhat to optimistic. However it shall be noted that the residual ε does not only include instrumental noise but also pseudo noise from representation errors.

In summary, we suggest that users who are interested in more realistic uncertainty estimates, shall apply the following error parameterization derived from the linear fit shown in **Figure 5.3**:

$$\sigma_{\text{corrected}}^{\text{XCO}_2} = \sigma_{\text{v09}}^{\text{XCO}_2} \cdot 1.361 - 0.133\text{ppm} \quad (5-2)$$

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 22
		Version 2
		26. Jan. 2021

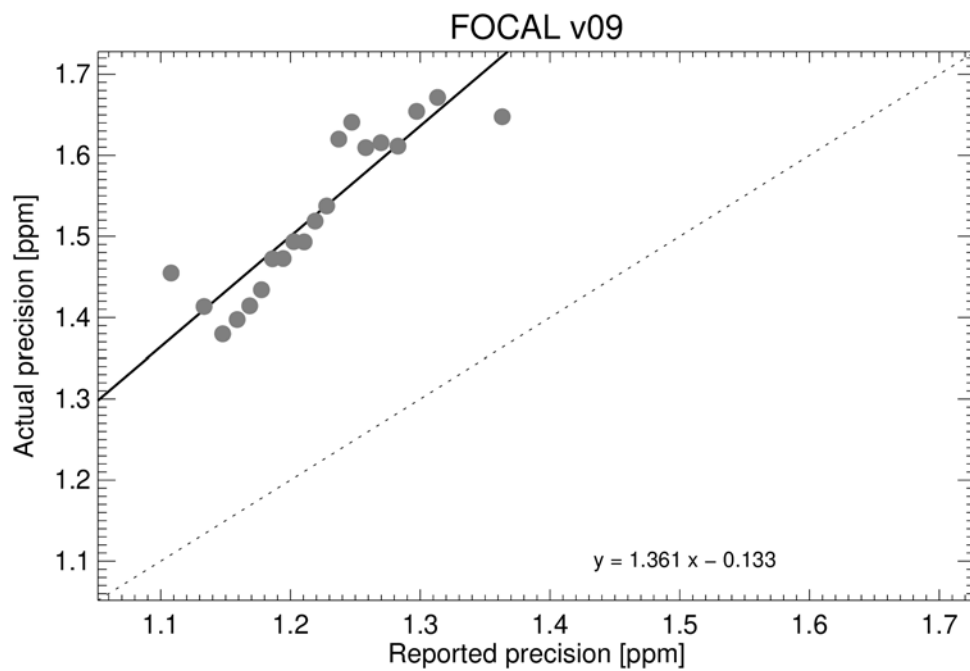


Figure 5.3: Reported uncertainty of FOCAL's optimal estimation retrieval vs. actual precision computed from the residual ε of the bias model of Section 5.1.

 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 23
		Version 2
		26. Jan. 2021

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 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 24
		Version 2
		26. Jan. 2021

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 GHG-CCI+ project	ESA Climate Change Initiative “Plus” (CCI+) End-to-End ECV Uncertainty Budget Version 2 (E3UBv2) - FOCAL OCO-2 for the Essential Climate Variable (ECV) Greenhouse Gases (GHG)	Page 25
		Version 2
		26. Jan. 2021

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